

Advanced Quantitative Research Methodology, Lecture

Notes: Robust Standard Errors¹

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What robust SEs are and are not

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- A better use for RSEs: as a test for misspecification

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Variance matrix unconstrained (includes covariances)

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Still allows for heteroskedasticity

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Standard linear-normal regression model assumptions

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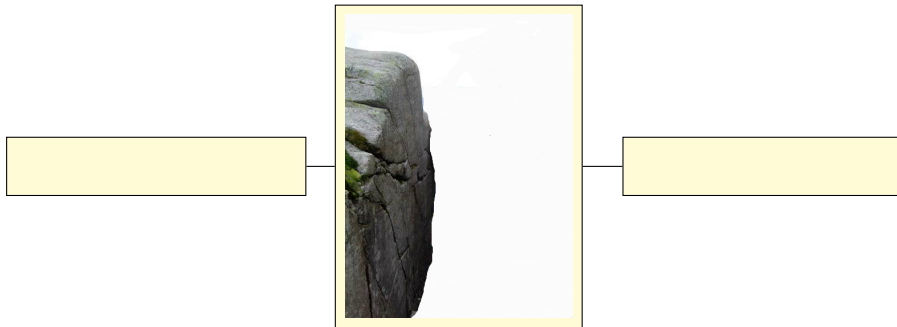
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 - The idea generalizes to any MLE model

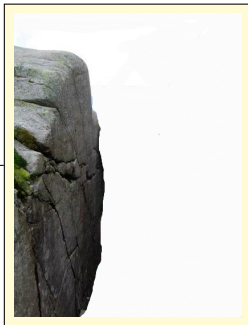
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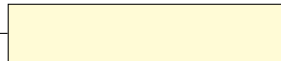
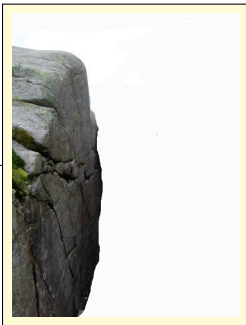
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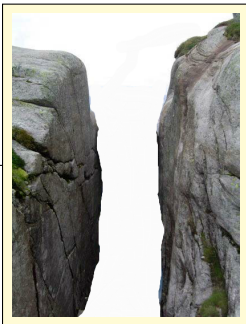
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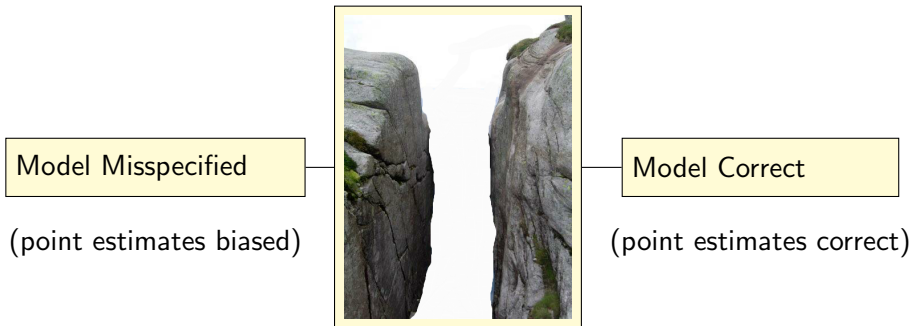
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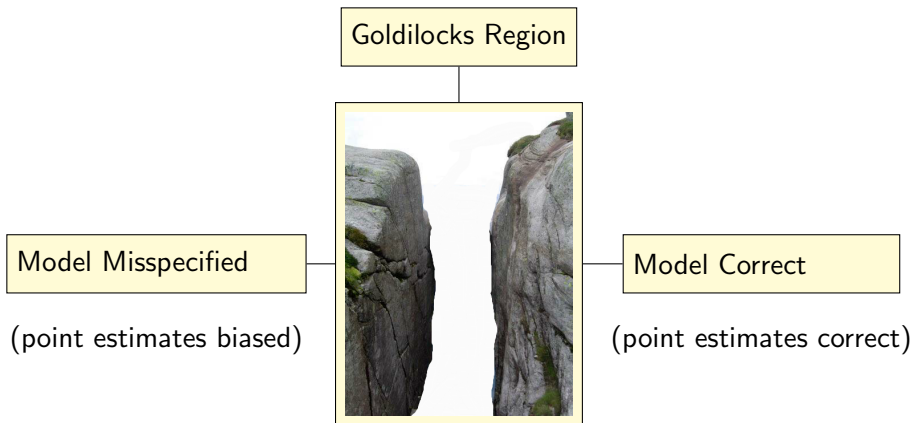


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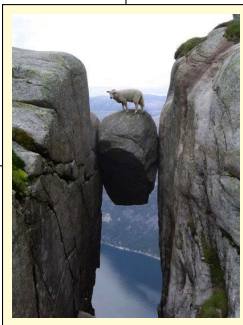


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Goldilocks Region



Model Misspecified

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Model Correct

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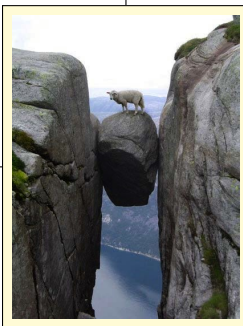
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Biased just enough to
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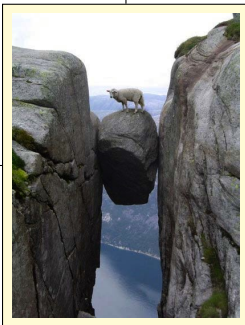
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 - We don't know: the substantive meaning of our results. How big are they, really?
 - We can't check: whether model implications are realistic.
- Parts of the model are wrong;



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- Only a few QOI's can be estimated.
 - Suppose DV: Democrat proportion of two-party vote.
 - We can estimate β , but not:
 - the probability the Democrat wins,
 - the variation in vote outcome,
 - or vote predictions with confidence intervals.
 - We don't know: the substantive meaning of our results. How big are they, really?
 - We can't check: whether model implications are realistic.
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- If $SE \neq RSE$: find misspecification, fix model, rerun until $SE = RSE$

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- Robust SE (0.34) $\approx$ classical SE (0.32)

Transformation of Y : Becomes Normal

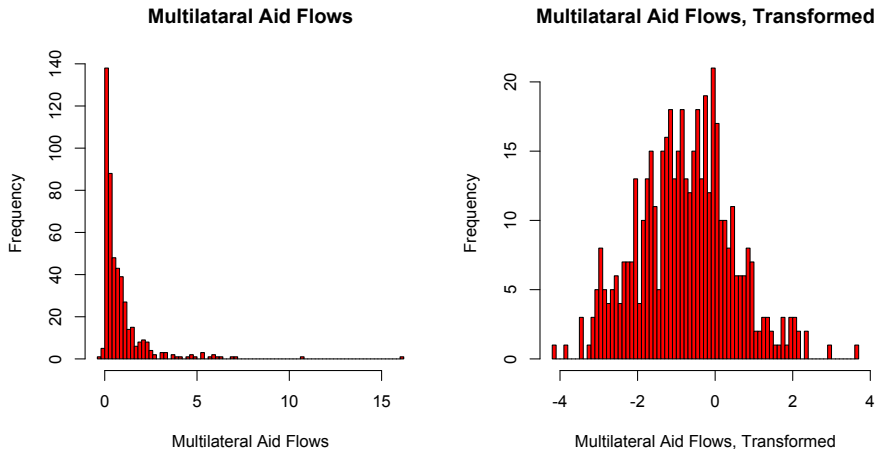
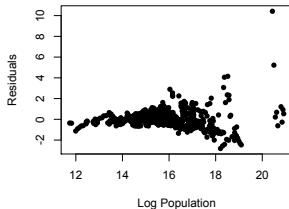


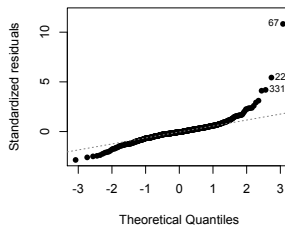
Figure: Distribution of the dependent variable before (left) and after (right) the Box-Cox transformation.

Transformation of Y : Removes Heteroskedasticity

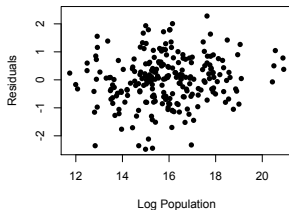
Population vs Residuals, Author's Model



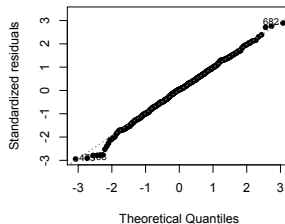
Q-Q Plot, Author's Model



Population vs Residuals, Altered Model



Q-Q Plot, Altered Model



Results: Transformed Model, Opposite Results

The misspecification $\rightsquigarrow$ bias, not inefficiency

